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# Physics Modelling: Mathematical Equations

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# Static characterization

$\Sigma$  forces for dynamic characterization modelling

$$TL = KTi - fw$$

$$i = 0.2323TL$$

$$\text{thus, } TL = KTi$$

$$KT = 4.305$$

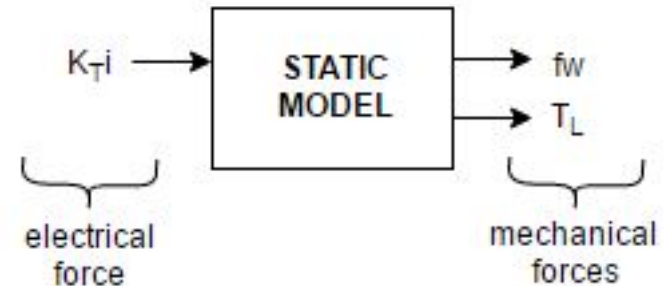
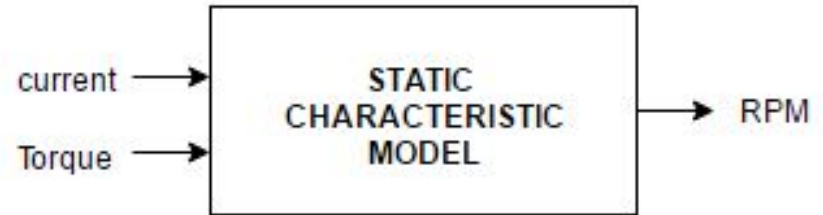
$$\text{substitute in TL eqn, } f = \frac{KT}{w} - \frac{TL}{w}$$

$$0.0056TL = \frac{4.305i}{w} - \frac{TL}{w}$$

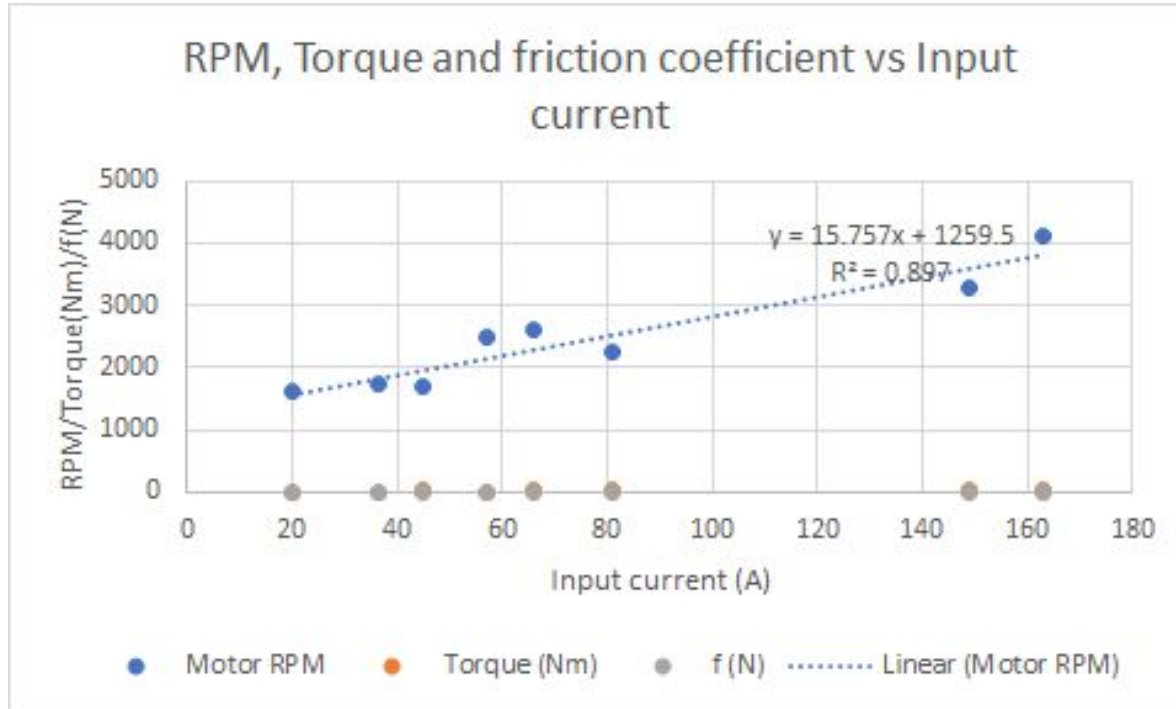
$$w = \frac{768.75i}{TL} - 178.57$$

Where

$KT$  is torque constant,  $w$  is motor speed in RPM,  $i$  is supply current,  $TL$  is load torque,  $f$  is friction coefficient



# Static model plot



With increase in input current, rpm has the biggest differential.

# Dynamic characterization

Σ forces for dynamic characterization modelling

$$J \frac{dw}{dt} = KTi - TL - fw$$

$$w = \frac{768.75i}{TL} - 178.57$$

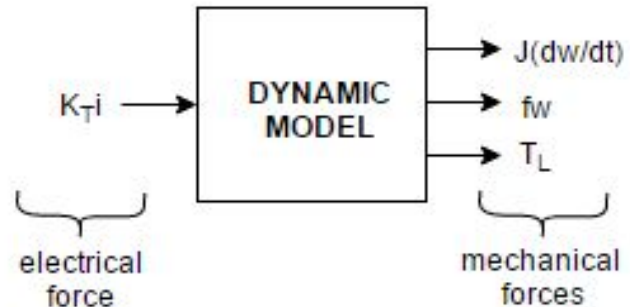
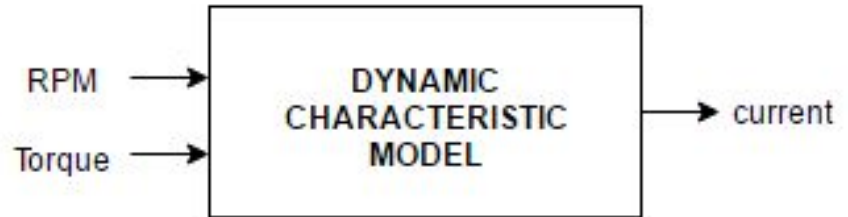
$$J \frac{dw}{dt} = \frac{768.75i}{TL} - 178.57 - w$$

$$w = \frac{76875i - 17857TL + ce^{\left(-\frac{500t}{3}\right)}}{100TL}$$

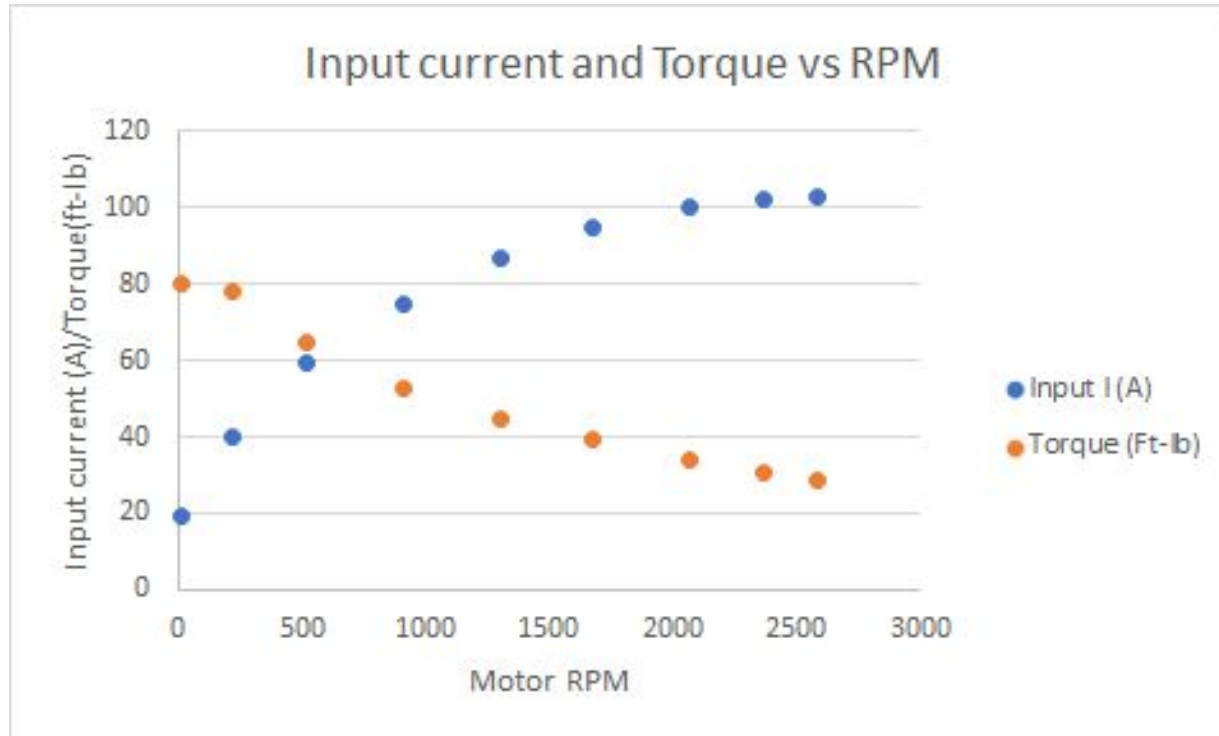
$$i = \frac{100TLw - ce^{\frac{500t}{3}} + 17857TL}{76875}$$

Where

$J$  is moment of inertia - .006,  $KT$  is torque constant,  $w$  is motor speed in RPM,  $i$  is supply current,  $TL$  is load torque,  $f$  is friction coefficient

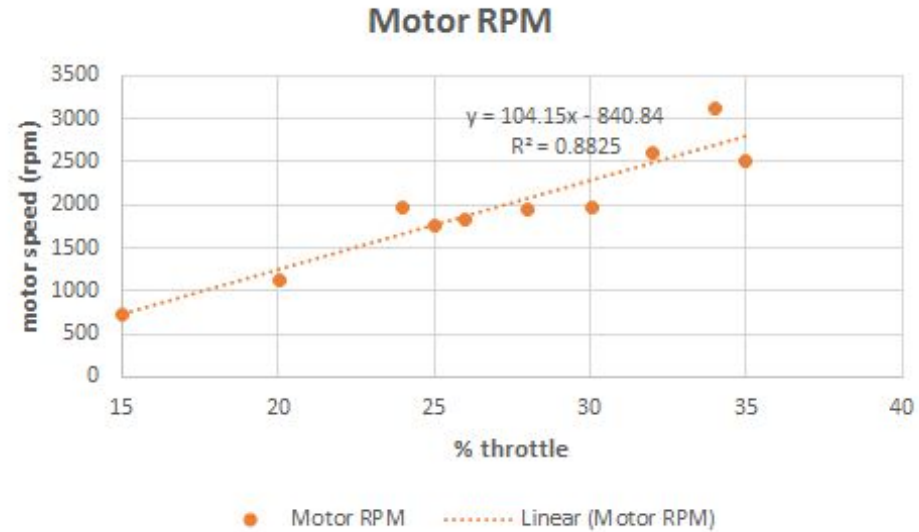
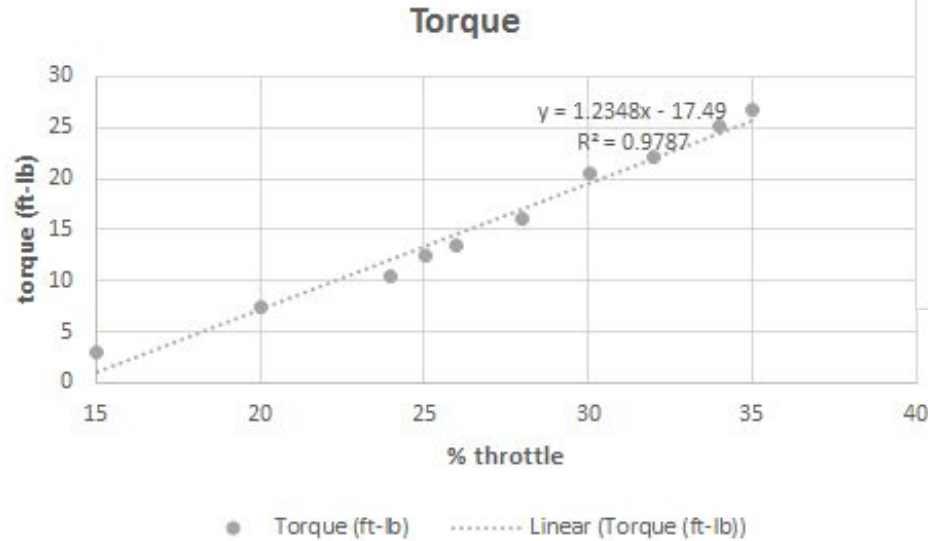


# Dynamic model plot



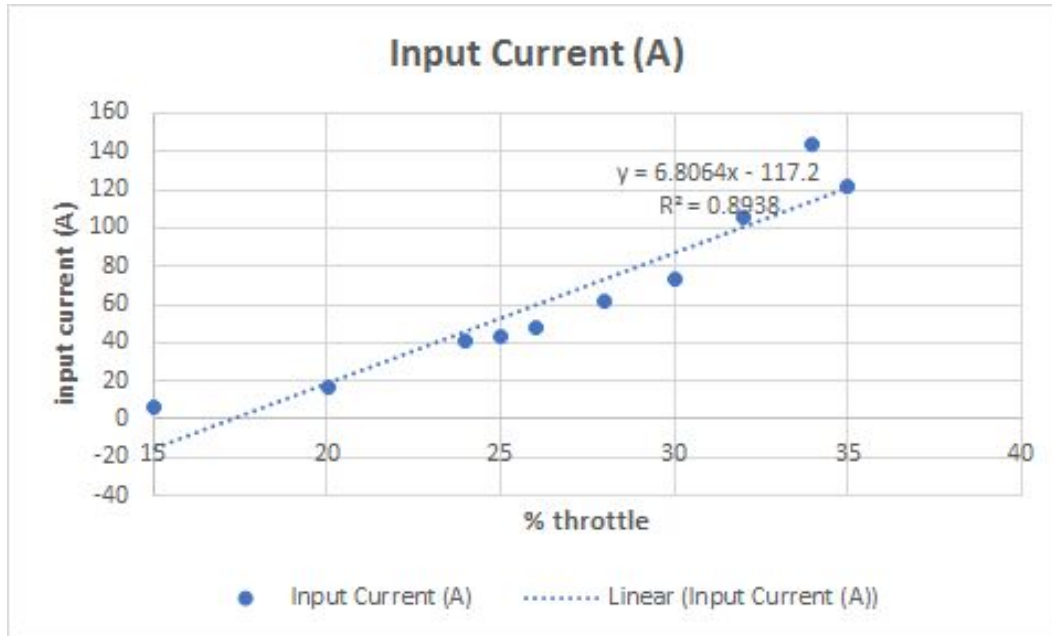
With increase in RPM, input current and torque depict an inverse relation, but have an optimum intersection point

# Pedal press to rpm and torque charac.



Torque and rpm parameters examined here have a direct proportionality relation with the % of max voltage. The R squared of the fits are high, supporting this result.

# Pedal press to current charac.



Input current parameter examined here have a direct proportionality relation with the % of max voltage. The R squared of the fits are high, supporting this result.

# Note on some model parameters

## Torque in eqn:

Torque used in transient calculations for dynamic model is a theoretical value.

Collect experimental data torque in a lab setup directly from the load cell. Then compare to theoretical values used.

## RPM vs % throttle:

Max motor RPM - 6500 RPM

1. Static model - 30% throttle, 90% load gives 4500 RPM
2. Dynamic model - 30% throttle, 90% load gives 3500 RPM

Note: various throttle % collected, but the above used because of max RPM at given setting of respective model



# Future work on equations

- Characterization of the motor and motor controller I/O for better approximation of system input and output power, to calculate the heat loss from this MCM system.

**Note:** Will be done in lab tomorrow (2/16/2017)